Comparing the Univariate Modeling Techniques for Measuring of Climate Index in Sitiawan, Malaysia

Sabri Ahmad, Shuhaili Safee

Abstract— The purpose of the article is to determine the most suitable technique to generate the forecast models using the data from the series of climate index in Sitiawan, Perak. This study are using univariate time series models consists of Naïve with Trend Model, Single Exponential Smoothing, DoubleExponential Smoothing, Holt's Method, Adaptive Response Rate Exponential Smoothing (ARRES) and Holt-winter's Trend and Seasonality Model. Using time-series data from 1961-2012 (monthly), there's several data consists missing/outlier value. The issues are overcome with applied the time series model for each missing values and then compare the measure error (mean square error, MSE) for each models. Then, the selection of the most suitable model was indicated by the smallest value of mean square error, MSE. Based on the analysis, Holtwinter's Trend & Seasonality model is the most suitable model for forecasting the climate index in Sitiawan, Perak.

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Index Terms— univariate time series models, climate index, mean square error (MSE)

1 INTRODUCTION

Forecasting is the whole process of developing the necessary methods to generate the future. As a decision-making tool, forecasting can act as a scanning device that captures the signals of the future outcomes based on either past events or other related factors considered to influence the outcome of event of interest. The information provided thus, would enable the firm to take the necessary actions to modify the existing plans to suite the expected changing environment so as to avoid following loss in revenues in the future.

A climate index defined as a calculated value that can be used to describe the changes and the state in the climate system. Climate indices allow a statistical study of variations of the dependent climatological aspects, such as analysis and comparison of time series, extremes, means, and trends. The prevalent research strategy in the climate-modelling community has been characterized by Knutti (2008), himself a climate modeller, as "take the most comprehensive model, run a few simulations at the highest resolution possible and then struggle to make sense of the result". The aim is to produce models as "realistic as possible: (Beven, 2002).

2 PROCEDURE

2.1 Materials and methods

The method of data collection is secondary data collection. The data was obtained via the NASA website. Due the period of time in Sitiawan station is longer from 1931 to 2012

(monthly) compare with the other station, then the data is se-

lected. But due to too many missing data, the study started with 1961 to 2012

Time series are very frequently plotted via line charts. The time series data can be Separation into components representing trend, seasonality, slow and fast variation, cyclical irregular.

UnivariateModelling Techniques divided into two categories is *naïve model* and *exponential smoothing techniques*. The analysis is divided by two categories which are estimation part (fitting part) and evaluation part (hold-out part).

The naïve trend model is modified to take this characteristic into account. The application of this model is fairly common among organizations. One reason for its popularity is that it can be used even with fairly short time series. The one step ahead forecast is represented as,

$$\mathbf{F}_{t+1} = \mathbf{Y}_t \left(\frac{\mathbf{Y}_t}{\mathbf{Y}_{t-1}} \right)$$

Where Y_t is the actual value at time t, and Y_{t-1} is the actual value in the preceding period. The initial value for this model is taking the first initial data from the actual data.

Exponential Smoothing Techniques:

i) *Single Exponential Smoothing Technique* is the simplest form of model within the family of the exponential smoothing techniques. The model requires only one parameter that is the smoothing constant, α , to generate the fitted values and hence the fitted model forecast for the next and all subsequent periods are determined by adjusting the current period forecast by

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a portion of the difference between the current forecast and the current actual value.

The equation for single exponential smoothed statistic is given as,

Where,

 $F_{t+m} = ay_t + (1-a)F_t$

 F_{t+m} is the single exponentially smoothed values in period t+m

This the actual value in time period t

 α is the unknown smoothing constant to be determined with value lying between 0 to 1 ($0 \le \alpha \le 1$)

 F_t is the forecast made in period t

ii) *Double exponential smoothing* this technique is also known as Brown's method. It is useful for series that exhibits a linear trend characteristic.To demonstrate the method the following notations will be used.

Let,

 S_t be the exponentially smoothed value of Y_t at time t

 $S^\prime{}_t\;$ be the double exponentially smoothed value of Y_t at time t

 $S_t = \alpha Y_t + (1-\alpha) S_{t-1}$

As usual, firstly input the initial values of the equation by using the equation below:

Follow by:

$$S'_{t} = \alpha Y_{t} + (1 - \alpha) S'_{t-1}$$
$$a_{t} = 2S_{t} - S'_{t}$$
$$b_{t} = \frac{\alpha}{1 - \alpha} (S_{t} - S'_{t})$$
$$F_{t+m} = a_{t} + b_{t} * m$$

This double exponential model requires only one parameter, which is smoothing constant, α , to generate the fitted values and hence forecast.

iii) *Holt's method*this technique not only smoothed the trend and the slope directly by using different smoothing constants but also provides more flexibility in selecting the rates at which the trend and slope are tracked. The application of the Holt's Method requires;

 $\begin{array}{l} \text{The exponential smoothed series: } S_t = \alpha Y_t + (1-\alpha) \left(St_{-1} + T_{t-1}\right) \\ \text{The trend estimate} \qquad : T_t = \beta \left(S_t - S_{t-1}\right) + (1-\beta) T_{t-1} \\ \text{Forecast m period into the future: } F_{t+m} = S_t + T_t * m \end{array}$

The α and β are the parameters to be determined with values ranging from 0 to 1.

iv) Adaptive Response Rate Exponential Smoothing (ARESS)The development of the adaptive response rate exponential smoothing (ARESS) technique is an attempt to overcome the problem that had discussed in all previous exponential

smoothing techniques by incorporating the effect of the changing pattern of the data series into the model.

The ARESS technique comprises of the following basic equations;

$$F_{t+m} = \alpha_t Y_t + (1 - \alpha) F_t$$

The value of α_t are estimated using the following equations;

$$\alpha_{t} = \frac{E_{t}}{AE_{t}}$$

where:

$$\begin{split} E_t &= \beta e_t + (1 - \beta) E_{t-1} \quad ; \ 0 \leq \beta \leq 1 \\ A E_t &= \beta |e_t| + (1 - \beta) A E_{t-1} \end{split}$$

And that,
$$e_t = Y_{t} - F_t$$

The value of E_t is defined as the smoothed average error, and AE_t is the smoothed absolute error.

Basically, this equation has similar meaning to the single exponential smoothing equation, except for the parameter value alpha (α_t) which is identified by the subscript t. in the application of the ARRES model one does not require to find the best alpha, α . This is because there is no single best α value which happens to vary over time. For this reason the appropriate symbol used is α_t .

v) *Holt-Winter's Trend and Seasonality* is one of the techniques that take into account the trend and seasonality factors. The Holt-Winter's Trend and Seasonality methodology consists of three basic equations: the level component, the trend component, and the seasonality component. The assumptions of multiplicative effect is been made with regard to the relationship of the components of data. On the assumption that the relationship of these components is multiplicative in nature, the equations are represented as follows:

Level Component: $L_t = \alpha(y_t/S_{t-s}) + (1-\alpha)(L_{t-1} + b_{t-1})$

Trend Component:

$$b_{t} = \beta (L_{t} - L_{t-1}) + (1 - \beta)b_{t-1}$$

Seasonality Component:

$$\begin{split} S_t &= \gamma \left(y_t / L_t \right) + (1 - \gamma) S_{t-s} \\ \text{The m-step-ahead forecast is calculated as:} \\ F_{t+m} &= (L_t + b_t \times m) S_{t-s+m} \end{split}$$

Selecting Best Forecasting Model Different models generally give different forecast values. A model that gives a very good fit is based on the smallest error measures.

Mean Squared Error (MSE) this measure is commonly used for comparing model's forecasting performance. It has the tendency to penalize large forecast errors more severally than other common accuracy measures and therefore is considered as the most appropriate measure to determine which methods avoid large errors. Let assume a series y₁,y₂,...,y₁ and the m-step-ahead forecasts made at time t be denoted by F t+m. Hence, for the one-step-ahead forecasts (for m=1) of any series, the MSE is written as:

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 $MSE = \sum_{t=1}^{n} e_{t+1}^2 / n$

Where: $e_{t+1}=y_{t+1} - y_{t+1}$ Where:

 y_{t+1} is the actual observation at the point t + 1

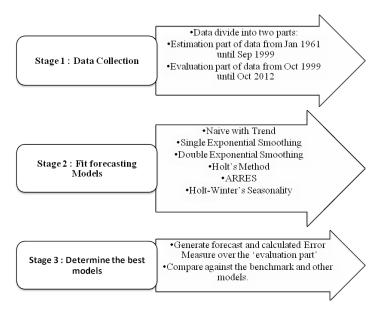
 F_{t+1} is the one-step-ahead forecast of y_{t+1} generated from the origin (t=1,2,3,..,n)

n is the number of out-of-sample terms generated by the model.

The data was separated into two parts. First part is called estimation and second part is called evaluation. Estimation part is 3 per 4 of data series, meanwhile for the rest is evaluation part. Since the total data series for climate index in Sitiawan is 622 series, 465 series was used for estimation part and 157 series for evaluation part.

Figure 1.1 display the estimation and evaluation procedure in this study. Basically, there are three stages involved:

- i) In this first stage, the series is divided into two parts. The first part is called model estimation part (fitted part) and the second part is the evaluation part (holdout part), which will be used to evaluate the model's forecasting performance.
- ii) In the second stage, the models are tested using various forms of functional relationship and variables selections
- iii) In the third stage, the minimum value of α , β and γ are determined by 'Solver' available in Microsoft Excel derived parameter values from data series for the related model. Then, all the models with the smallest MSE are evaluated by comparing the MSE value of each model.
- iv) The model that meets all the criteria is thus selected as the most suitable model. The selection criterion is based on the results of comparing their respective error measures.



Climate index

Figure 1.1: Estimation and Evaluation Procedures of Forecast-

ing Model

2 Results and discussions

Fig 1,the actual graph of climate index, Sitiawan. The data is not stationary, because there is trend line (upward trend) appear. By looking at the flow of the data, there is wave like pattern in the graph, so the data is seasonal.

Table 2 MSE values by type of model			
	MSE	MSE	
	(without	(After compute	
Model type	missing val-	all the missing	
	ue: 1961-	values: 1961-	
	2000)	2012)	
naive with trend	0.347814	0.377956	
single explonential smoothing	0.1747	0.179325	
double exponential smoothing	0.187777	0.232588	
Holt's Method	0.173667	0.178537	
ARRES	0.175708	0.181282	
Holt-winter's Trend & Sea- sonal	0.107317	0.109894	

By using MSE to identify the smallest error, the model of Holtwinter's Trend & Seasonal is the best due to value MSE without missing value and MSE after compute all missing values are smallest compare MSE of the other model.

Using the complete data (without missing values), the estimations were done with the objective of minimising Mean Squared Error (MSE). Results of the corresponding MSE value and graft (evaluation part) for each model are shown below

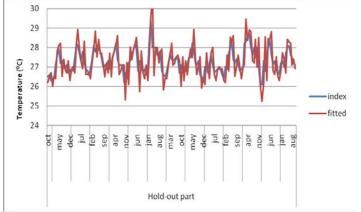


Fig 2 The Naïve with Trend graph of climate index, Sitiawan

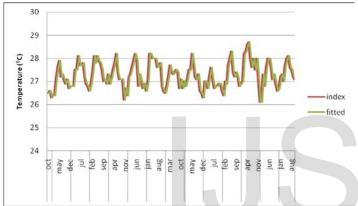


Fig 3 The Single Exponential Smoothinggraph of climate index, Sitiawan

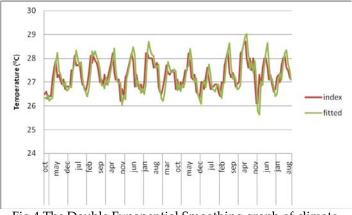


Fig 4 The Double Exponential Smoothing graph of climate index, Sitiawan

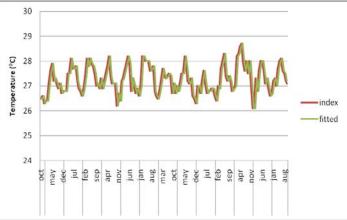
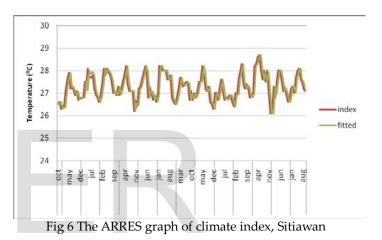
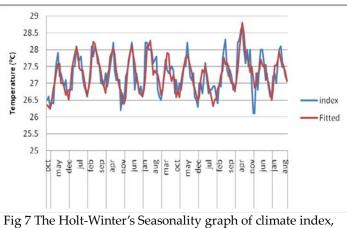


Fig 5 The Holt's Method graph of climate index, Sitiawan





Sitiawan

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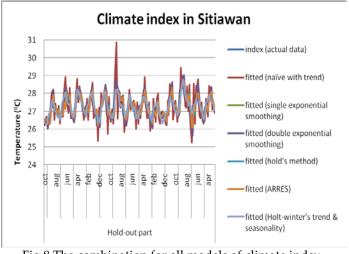


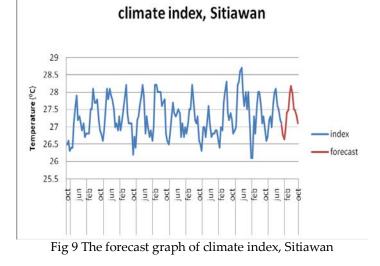
Fig 8 The combination for all models of climate index, Sitiawan

Table 3: Comparison of MSE		
	MSE	MSE
Model type		Hold-out
	Fitting part: (1961-1999)	part: (2000-2012)
naive with trend	0.3515	0.4562
single explonential smoothing	0.1766	0.1874
double exponential smoothing	0.2278	0.2469
Holt's Method	0.1755	0.1874
Adaptive Response Rate Exponential Smoothing	0.1778	0.1901
Holt-winter's Trend & Sea- sonality	0.1083	0.1102

The criterion used to differentiate between a poor forecast model and good forecast model is called 'error measure'. Based on the error measures as shown in Table 3, Holt-winter's Trend & Seasonality has the lowest value of MSE for estimation part (fitting part) and evaluation part (hold-out part) with the value of MSE is 0.1083 and 0.1102.

3 CONCLUSION

Based on the one step ahead forecast analysis, Holt-winter's Trend & Seasonality Model is the mostsuitable model for forecasting of Climate index in Sitiawan since the value of MSE is smallest compare with other models for both estimation and evaluation part. Using the solver in Microsoft excel, the value for α = 0.444, β =0.005 and γ =0.162. The forecast value for best model are shown as



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